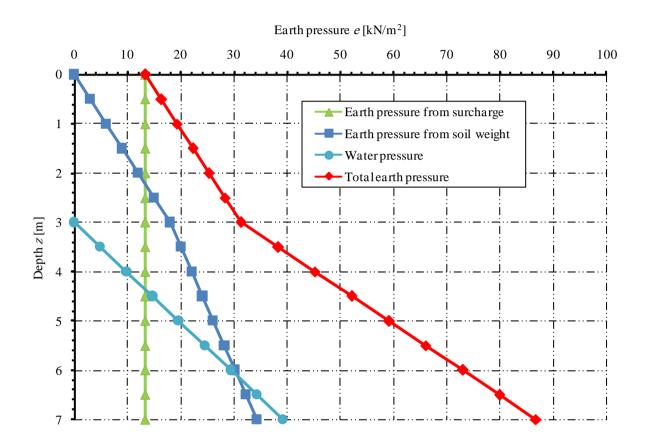
Lateral Earth Pressure by the Program GEO Tools



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Preface

Various problems in Geotechnical Engineering can be investigated by the program *GEO Tools*. The original version of the program *GEO Tools* in the *GEOTEC Office* package was developed by Prof. M. Kany, Prof. M. El Gendy and Dr. A. El Gendy. After the death of Prof. Kany, Prof. M. El Gendy and Dr. A. El Gendy further developed the program to meet the needs of practice.

This book describes the essential equations used in *GEO Tools* to obtain the lateral earth pressure on the retaining structures with some verification examples. *GEO Tools* is a simple user interface program and needs little information to define a problem.

1 Lateral Earth Pressure

1.1 Lateral Active Earth Pressure

Lateral earth pressure is the pressure that soil exerts in the horizontal direction. Lateral active earth pressure at point *A* in the soil is equal to the effective vertical stress σ'_{ν} multiplied by a coefficient, $\sigma_h = k_a \sigma'_{\nu}$. If a water table exists, horizontal hydrostatic water pressure is considered. Lateral water pressure at point *A* in the soil is the weight of the water column above that point $w = \gamma_w z$.

1.2 Defining the project data

1.2.1 Firm Header

When printing the results, the main data (firm name) are displayed on each page at the top in two lines. The firm name can be defined, modified, and saved using the "Firm Header" option from the setting tab (see Figure 1).

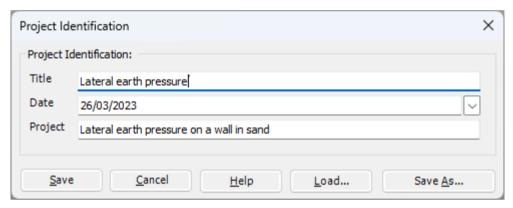


Figure 1 Firm Header

1.2.2 Task of the program *GEO Tools* (Analysis Type)

The *GEO Tools* program can be used to analyze various problems in Geotechnical Engineering for shallow and deep foundations, Figure 2.

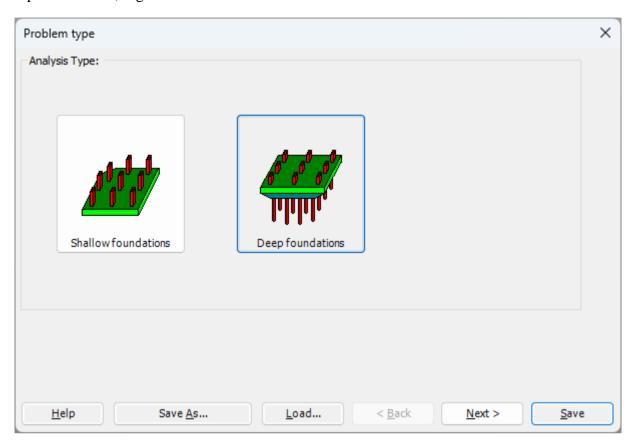


Figure 2 Problem type

According to the main menu (Figure 3), the following geotechnical problems can be analyzed for shallow foundations:

- 1. Analysis of an axially and laterally loaded single pile (Mindlin's solution)
- 2. Analysis of laterally loaded single pile by p-y curve
- 3. Analysis of laterally loaded single pile (elastic embedded pile)
- 4. Bearing capacity and settlement of single pile or pile wall
- 5. Analysis of a combined piled raft
- 6. Stress coefficients according to GEDDES
- 7. Sheet pile wall
- 8. Analysis of single barrette
- 9. Analysis of a barrette raft
- 10. Lateral earth pressure
- 11. Effective vertical stress
- 12. Analysis of a monopole

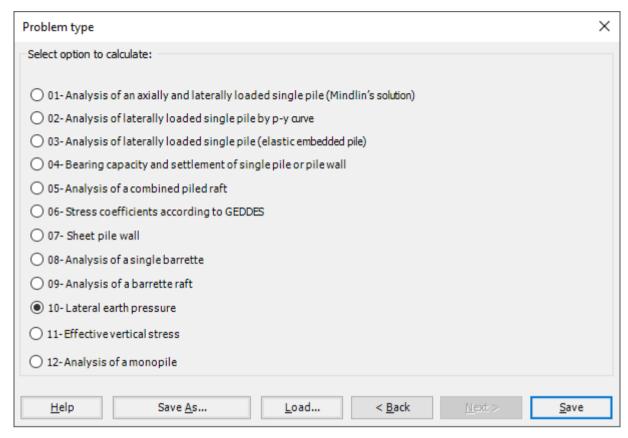


Figure 3 Problem type for shallow foundation

In the menu of Figure 3, select the option:

10-Lateral earth pressure

The following paragraph describes how to determine the lateral earth pressure by using the program *GEO-Tools*. The input data are the geometry of the wall, load intensity, and soil properties.

1.2.3 Project Identification

In the program, it must be distinguished between the following two data groups:

- System data (For identification of the project that is created and information to the output for the printer).
- 2 Soil data (Soil properties and so on).

The defining input data for these data groups is carried out as follows:

After clicking on the "Project Identification" option, the following general project data are defined (Figure 4):

Title: Title label

Date: Date

Project: Project label

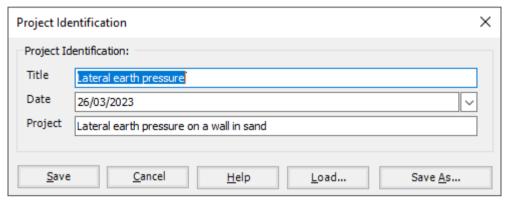


Figure 4 Project Identification

1.2.4 Lateral earth pressure

After clicking on the "Lateral earth pressure" option, the following data for determining the lateral earth pressure are defined (Figure 5):

Load intensity and water:

q Distributed load [kN]

Gw Ground water depth [m]

Element/Width of Working Area:

Dz Depth increment in z-direction [m]

Bw Width of working area [m]

Soil data:

Layer:

c Cohesion of the soil, $[kN/m^2]$

φ Angle of internal friction of the soil, [°]

 γ_d Dry unit weight of the soil, [kN/m³]

 γ_{sat} Saturated unit weight of the soil, [kN/m³]

h Layer thickness [m]

Soil type

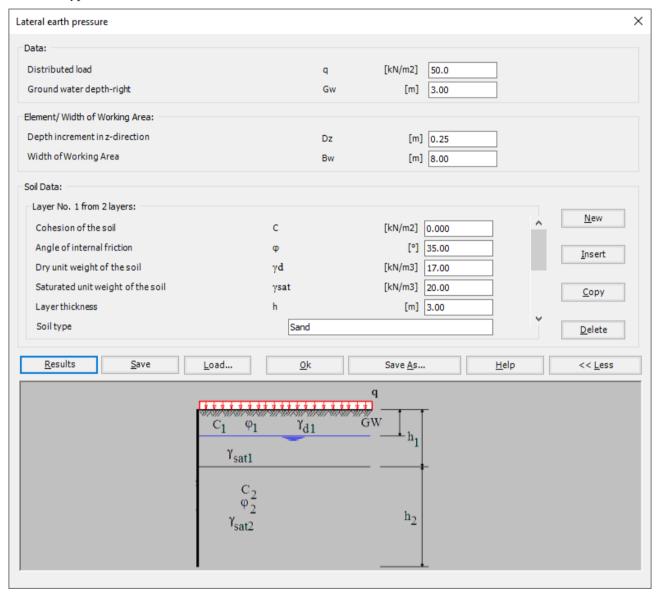


Figure 5 Lateral earth pressure

1.3 Examples to verify Lateral Earth Pressure

1.3.1 Introduction

The application possibilities of the program *GEO Tools* to obtain the lateral earth pressure on the retaining structures are presented below in some numerical examples. Examples were carried out to verify and test the application of the analytical and numerical proposed procedures outlined in this book.

1.3.2 Example 1: Lateral earth pressure on a wall in sand

1.3.2.1 Description of the problem

For the given wall in sand Figure 6, determine per meter the following:

- Lateral earth pressure on the wall
- Lateral water pressure on the wall
- Lateral earth pressure on the wall due to a surface surcharge load
- Total horizontal force on the wall.

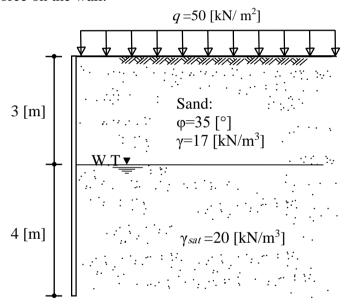


Figure 6 Wall in Sand

1.3.2.2 Lateral Active Earth Pressure

Lateral active earth pressure at point *A* in the soil is equal to the effective vertical stress σ'_{ν} multiplied by a coefficient, $\sigma_h = k_a \sigma'_{\nu}$. If a water table exists, horizontal hydrostatic water pressure is considered. Lateral water pressure at point *A* in the soil is the weight of the water column above that point $w = \gamma_w z$.

Coefficient of lateral active earth pressure is given by:

$$k_a = \frac{1 - \sin 35}{1 + \sin 35} = 0.27$$

The determination of the lateral active earth pressure σ_a is tabulated in 0 and plotted in Figure 7 and Figure 8, while the total lateral earth pressure forces are plotted in Figure 9 and Figure 10.

Table 1 Determination of lateral active earth pressure with depth

1 aoic 1	Determination of fateral active (carm pressure with depth	
Depth	lateral active earth pressure	Hydrostatic water	Total lateral active
z		pressure	earth pressure
[m]	$\sigma_a = k_a \sigma'_v$	$w = \gamma_w z$	$E=\sigma_a+w$
	$[kN/m^2]$	[kN/m ²]	[kN/m ²]
3	$\sigma_{a1} = k_a \sigma'_{v1} = 0.27 \times 51 = 13.77$	0	13.77
7	$\sigma_{a2} = k_a \ \sigma'_{v2} = 0.27 \times 91.76 = 24.78$	$w = \gamma_w h_2 = 9.81 \times 4 = 39.24$	64.02

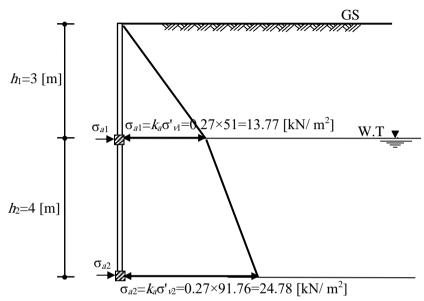


Figure 7 Lateral active earth pressure σ_a

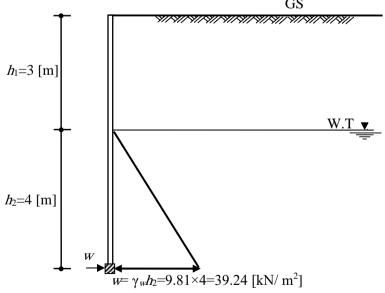


Figure 8 Hydrostatic pressure w

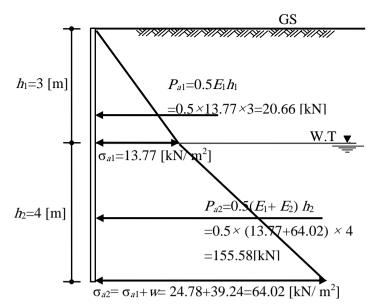


Figure 9 Total lateral earth pressure σ_a and active forces P_a

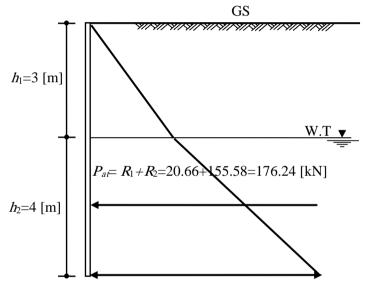


Figure 10 Total horizontal force on the wall P_{at}

1.3.2.3 Lateral earth pressure with a surface surcharge load (fill)

Since the surcharge load (fill) covers an extensive area on the surface, the lateral earth pressure at any point *A* in the soil increases by $k_a q = 0.27 \times 50 = 13.5 \text{ [kN/m}^2]$ due to the weight of the fill, Table 2 and Figure 11.

Table 2 Determination of lateral active earth pressure with depth

Depth	Layer thickness	lateral active earth pressure
z	h	$\sigma_a = k_a \ q + E$
[m]	[m]	$[kN/m^2]$
3	3	$\sigma_{a1} = k_a \ q + k_a \ \sigma'_{v1} = 0.27 \times 50 + 13.77 = 27.27$
7	4	$\sigma_{a2} = k_a \ q + k_a \ \sigma'_{v2} = 0.27 \times 50 + 64.02 = 77.52$

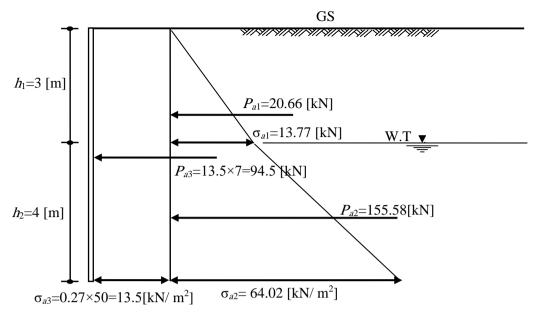


Figure 11 Total lateral earth pressure σ_a and active forces P_a

Figure 12 shows the earth pressures and water presser in a single view

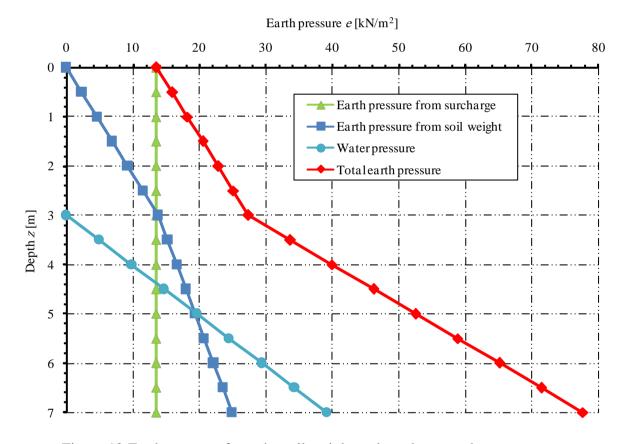


Figure 12 Earth pressure from the soil weight and surcharge and water pressure

1.3.2.1 Lateral earth pressure on a wall in sand by GEO Tools

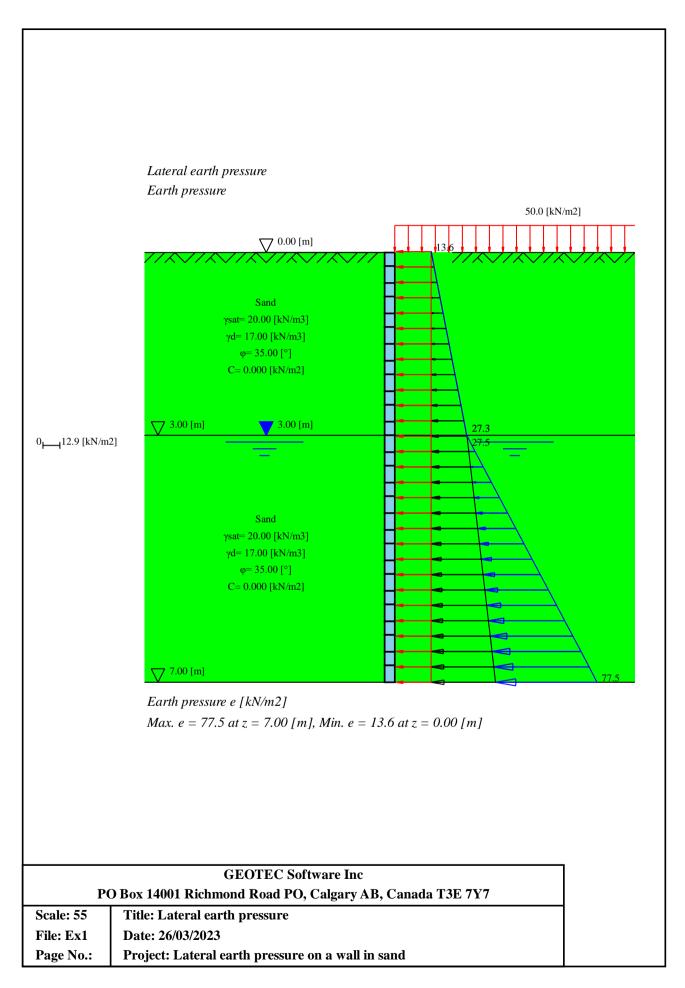
The lateral earth pressure on a wall in sand obtained by *GEO Tools* is equal to that obtained by hand calculation. Also, the input data and results of GEO Tools for this example are presented on the next pages.

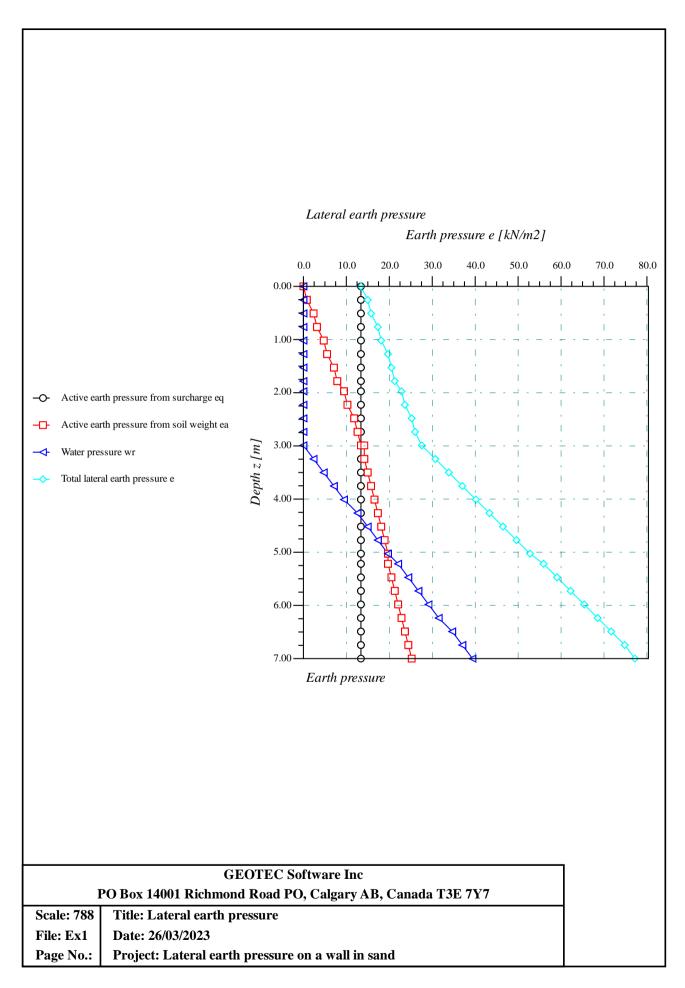
GEO Tools Version 13 Program authors M. El Gendy/ A. El Gendy ************************************				
Lateral earth pressure				
Data: Distributed load Total thickness of soil layers	q Ht	[kN/m2] [m]		
Element size/ Width of Working Area: Element size Width of Working Area	Dz Bw	[m] [m]	= 0.25 = 8.00	
Soil Data: Ground water depth	Gwl	[m]	= 3.00	
Layer No.: 1 Cohesion of the soil Angle of internal friction Dry unit weight of the soil Saturated unit weight of the soil Layer thickness Soil type	C φ γd γsat h BOD	[°] [kN/m3] [kN/m3] [m]	= 0.000 = 35.00 = 17.00 = 20.00 = 3.00 = Sand	
Layer No.: 2 Cohesion of the soil Angle of internal friction Dry unit weight of the soil Saturated unit weight of the soil Layer thickness Soil type	C φ γd γsat h BOD	[°] [kN/m3] [kN/m3] [m]	= 0.000 = 35.00 = 17.00 = 20.00 = 4.00 = Sand	

Result: Resultant R [kN] = 271.8 Location of the resultant from the wall base Y [m] = 2.50

Earth pressures on the sheet pile:

			pressure from surcharge	earth pressure from surcharge	earth pressure from soil	earth pressure from soil	pressure	Water pressure	lateral earth	lateral
[-]	[m]	[m]	q1 [kN/m2]	[kN/m2]	[kN/m2]	[kN/m2]	[kN/m2]	[kN/m2]	σ'1 [kN/m2]	[kN/m2]
1	0.00	0.25	13.5	12 5		1 2			12 6	117
	0.25	0.50	13.5							15.9
3	0.50	0.75		13.5						
4	0.75	1.00		13.5						
5	1.00	1.25		13.5					18.2	
6	1.25	1.50	13.5	13.5	5.8	6.9	0.0	0.0	19.3	
7	1.50	1.75	13 5	13 5	6 9	8 1	0 0	0.0	20.5	21.6
8	1.75	2.00	13.5 13.5 13.5 13.5 13.5	13.5	8 1	9 2	0 0	0 0	21 6	22.8
9	2.00	2.25	13.5	13.5	9.2	10.4 11.5 12.7 13.8 14.5	0.0	0.0	22.8	23.9
10	2.25	2.50	13.5	13.5	10.4	11.5	0.0	0.0	23.9	25.1
11	2.50	2.75	13.5	13.5	11.5	12.7	0.0	0.0	25.1	
12	2.75	3.00	13.5	13.5	12.7	13.8	0.0	0.0	26.2	
13	3.00	3.25	13.5	13.5	13.8	14.5	0.1	2.5	27.5	
14	3.25	3.50	13.5	13.5	14.5	15.2	2.5	4.9	30.5	
15	3.50	3.75		13.5		15.9	4.9	7.4	33.7	
16	3.75	4.00		13.5			7.4			
17	4.00	4.25		13.5			9.8			
18	4.25	4.50		13.5			12.3			
19	4.50	4.75		13.5		18.7				
20	4.75	5.00				19.3				
21	5.00	5.25		13.5		20.0				
22	5.25	5.50				20.7	22.1	24.5		
23	5.50	5.75	13.5			21.4	24.5	27.0	58.8	
24	5.75	6.00	13.5			22.1	27.0	29.4	61.9	
25	6.00	6.25	13.5	13.5	22.1	22.8	29.4	31.9	65.1	
26	6.25	6.50	13.5	13.5	22.8	23.5	31.9 34.3	34.3	68.2	
27 28	6.50 6.75	6.75 7.00	13.5	13.5 13.5 13.5	23.5	24.2	34.3	34.3 36.8 39.1	71.4 74.5	
∠8	6.75	7.00	13.5	13.5	24.2	24.8	36.8	39.1	/4.5	//.5





1.3.3 Example 2: Lateral earth pressure for layered soil (with cohesion)

1.3.3.1 Description of the problem

For the given soil profile of three layers in Figure 13, determine the lateral earth pressure on the wall.

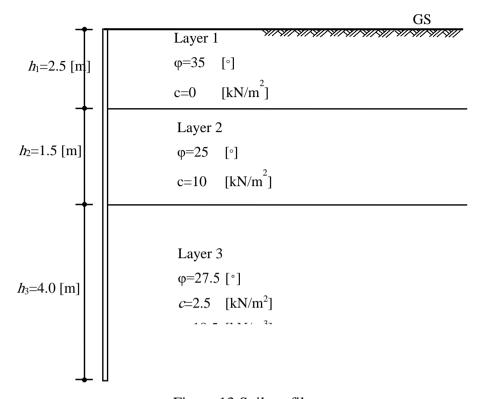


Figure 13 Soil profile

1.3.3.2 Lateral earth pressure on a wall in sand by GEO Tools

The lateral earth pressure on a wall for the three layers obtained by *GEO Tools* for this example are presented on the next pages.

GEO Tools Version 13

Program authors M. El Gendy/ A. El Gendy

Title: Lateral earth pressure

Date: 26/03/2023

Project: Lateral earth pressure for layered soil (with cohesion)

File: Ex2

Lateral earth pressure

Dat	l-a	٠

Layer No.: 3

Layer thickness Soil type

Cohesion of the soil

Angle of internal friction

Dry unit weight of the soil

Saturated unit weight of the soil

Data: Distributed load Total thickness of soil layers	q Ht	[kN/m2] [m]		
Element size/ Width of Working Area: Element size Width of Working Area	Dz Bw	[m] [m]		
Soil Data: Ground water depth	Gwl	[m]	=	8.00
Layer No.: 1 Cohesion of the soil Angle of internal friction Dry unit weight of the soil Saturated unit weight of the soil Layer thickness Soil type	γsat h		= = =	35.00 19.00 18.81 2.50
Layer No.: 2 Cohesion of the soil Angle of internal friction Dry unit weight of the soil Saturated unit weight of the soil Layer thickness Soil type	•	[kN/m3] [kN/m3] [m]	= =	25.00 17.00 16.61 1.50

C [kN/m2] = 2.500

 $\gamma d [kN/m3] = 18.50$ ysat [kN/m3] = 18.31

h = [m] = 4.00 BOD = [-] = Sand

φ

[°] = 27.50

Lateral Earth Pressure

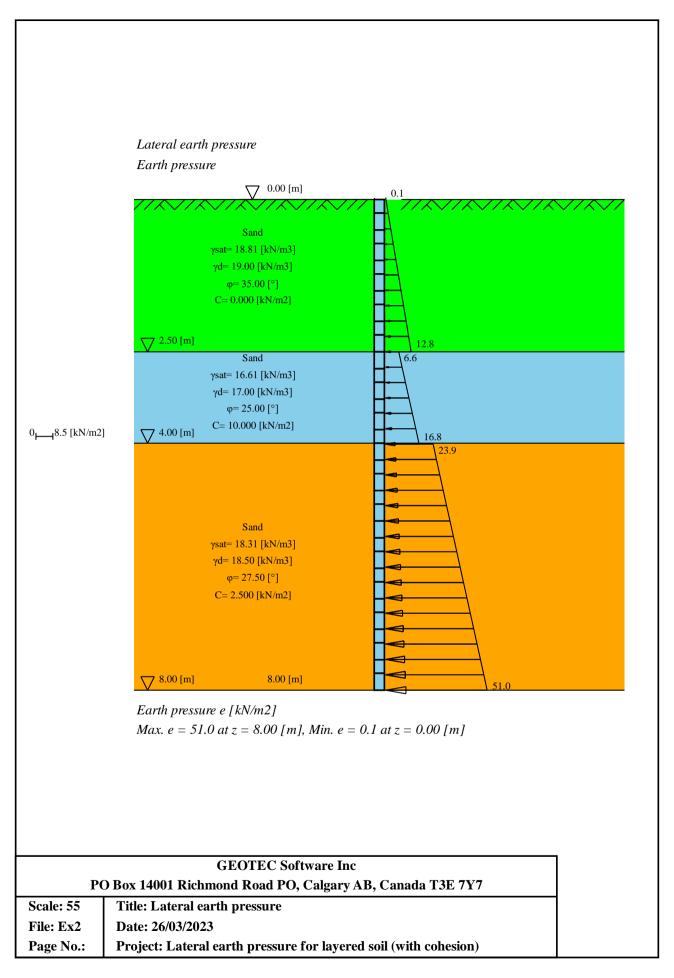
Result:

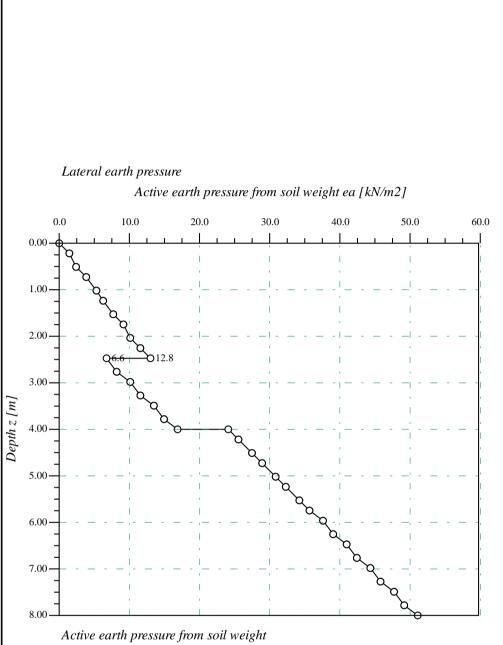
Resultant Resul

Earth pressures on the sheet pile:

Eart	n press	ures on	the sheet	pile:			
			Active earth pressure from soil	Active earth pressure	Total lateral earth pressure	Total lateral earth	
I	z1	z2	σz1	σz2	σ'1	σ'2	
						[kN/m2]	
	0.00 0.25 0.50 0.75 1.00 1.25 1.50 2.25 2.50 2.75 3.00 3.25 3.50 3.75 4.00 4.25 4.50 4.75 5.00 5.25 5.50 5.75	0.25 0.50 0.75 1.00 1.25 1.50 1.75 2.00 2.25 2.75 3.00 3.25 3.50 3.75 4.00 4.25 4.50 4.75 5.00 5.25 5.50 5.75	0.1 1.3 2.6 3.9 5.1 6.4 7.7 9.0 10.3 11.6 6.6 8.3 10.0 11.7 13.4 15.2 23.9 25.5 27.3 29.0 30.7 32.4 34.1 35.8	1.3 2.6 3.9 5.1 6.4 7.7 9.0 10.3 11.6 12.8 8.3 10.0 11.7 13.4 15.2 16.8 25.5 27.3 29.0 30.7 32.4 34.1 35.8 37.5	0.1 1.3 2.6 3.9 5.1 6.4 7.7 9.0 10.3 11.6 6.6 8.3 10.0 11.7 13.4 15.2 23.9 25.5 27.3 29.0 30.7 32.4 34.1 35.8	1.3 2.6 3.9 5.1 6.4 7.7 9.0 10.3 11.6 12.8 8.3 10.0 11.7 13.4 15.2 16.8 25.5 27.3 29.0 30.7 32.4 34.1 35.8 37.5	
26 27 28 29 30 31 32	6.25 6.50 6.75 7.00 7.25 7.50	6.50 6.75 7.00 7.25 7.50 7.75	39.2 40.9 42.6 44.3 46.0 47.7	40.9 42.6 44.3 46.0 47.7 49.4	39.2 40.9 42.6 44.3	40.9 42.6 44.3 46.0 47.7 49.4	

-20-





Max. ea = 51.0 [kN/m2] at z = 8.00 [m], Min. ea = 0.1 [kN/m2] at z = 0.00 [m]

GEOTEC Software Inc					
]	PO Box 14001 Richmond Road PO, Calgary AB, Canada T3E 7Y7				
Scale: 482	Title: Lateral earth pressure				
File: Ex2	Date: 26/03/2023				
Page No.:	Project: Lateral earth pressure for layered soil (with cohesion)				

1.3.4 Example 3: Lateral earth pressure for layered soil (without cohesion)

1.3.4.1 Description of the problem

For the given soil profile of three layers in Figure 13, determine the lateral earth pressure on the wall.

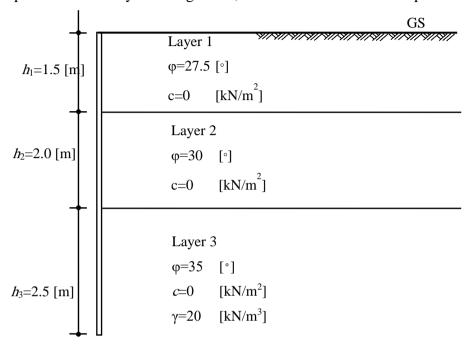


Figure 14 Soil profile

1.3.4.2 Lateral earth pressure on a wall in sand by GEO Tools

The lateral earth pressure on a wall for the three layers obtained by *GEO Tools* for this example are presented on the next pages.

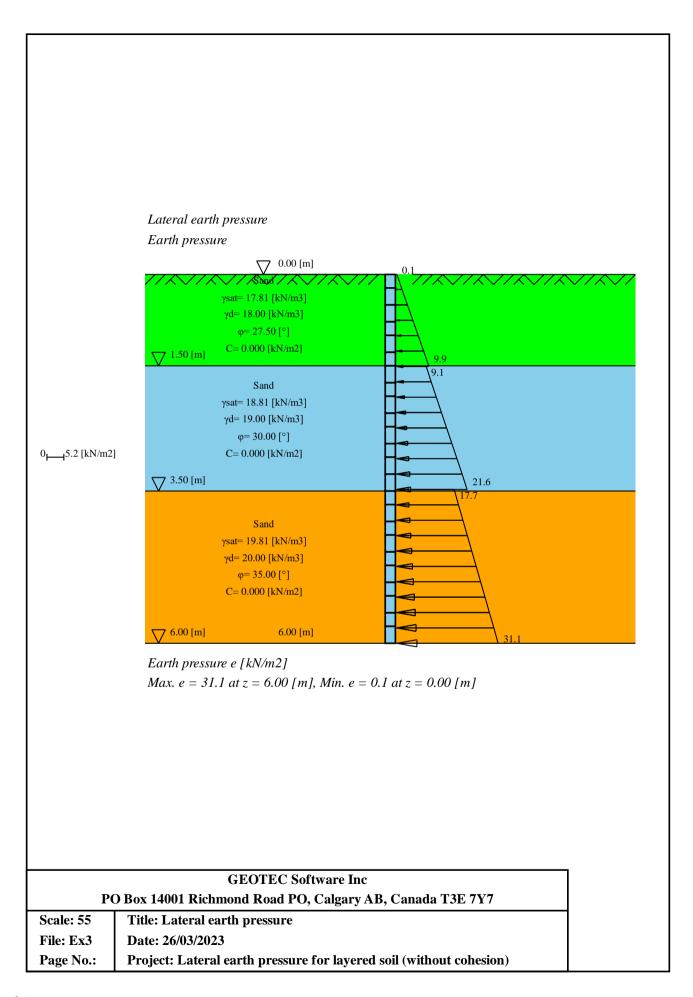
************ GEO Tools Version 13 Program authors M. El Gendy/ A. El Gendy Title: Lateral earth pressure Date: 26/03/2023 Project: Lateral earth pressure for layered soil (without cohesion) File: Ex3 Lateral earth pressure Data: [m] = 6.00Element size/ Width of Working Area: Dz [m] = 0.25 Bw [m] = 8.00 Element size Width of Working Area Soil Data: Ground water depth Gwl [m] = 6.00Layer No.: 1 Cohesion of the soil С [kN/m2] = 0.000Angle of internal friction Dry unit weight of the soil Saturated unit weight of the soil Layer thickness Soil type Layer No.: 2 C [kN/m2] = 0.000 ϕ [°] = 30.00 γd [kN/m3] = 19.00Cohesion of the soil Dry unit weight of the soil Saturated unit weight of the soil $\begin{array}{lll} \text{Ysat } \lfloor kN/m \text{J} - \text{I...} \\ \text{h} & [m] & = 2.00 \\ \text{ROD } [-] & = \text{Sand} \end{array}$ $\gamma sat [kN/m3] = 18.81$ Layer thickness Soil type Layer No.: 3 C = [kN/m2] = 0.000Cohesion of the soil Dry unit weight of the soil Saturated unit weight of the soil Layer thickness

Soil type

Result: Resultant R [kN] = 99.3 Location of the resultant from the wall base Y [m] = 2.11

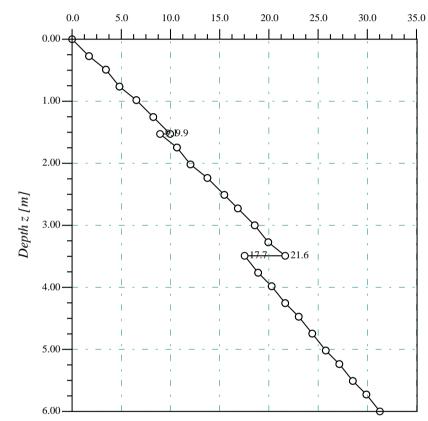
Earth pressures on the sheet pile:

No. Depth Depth Active arth earth lateral lateral pressure pressure soil soil weight weight [kN/m2] [kN/m2] [kN/m2] [kN/m2] [kN/m2] [x 0.25 0.50 1.7 3.3 1.7 3.3 3 0.50 0.75 3.3 5.0 3.3 5.0 4 0.75 1.00 5.0 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 6.6 8.3 9.9 8.3 9.9 7 1.50 1.75 9.1 10.6 9.1 10.6 8 1.75 2.00 10.6 12.2 10.6 12.2 9 2.00 2.25 12.2 13.7 12.2 13.7 10 2.25 2.50 13.7 15.3 11.7 15.3 11. 2.50 2.75 15.3 16.9 15.3 16.9 12. 2.75 3.00 16.9 18.5 20.1								
1 0.00 0.25 0.1 1.7 0.1 1.7 2 0.25 0.50 1.7 3.3 1.7 3.3 3 0.50 0.75 3.3 5.0 3.3 5.0 4 0.75 1.00 5.0 6.6 5.0 6.6 5 1.00 1.25 6.6 8.3 6.6 8.3 6 1.25 1.50 8.3 9.9 8.3 9.9 7 1.50 1.75 9.1 10.6 9.1 10.6 8 1.75 2.00 10.6 12.2 10.6 12.2 9 2.00 2.25 12.2 13.7 12.2 13.7 10 2.25 2.50 13.7 15.3 13.7 15.3 11 2.50 2.75 15.3 16.9 15.3 16.9 12 2.75 3.00 16.9 18.5 16.9 18.5	I [-]	z1 [m]	z2 [m]	earth pressure from soil weight σz1 [kN/m2]	earth pressure from soil weight σz2 [kN/m2]	lateral earth pressure $\sigma'1\\[kN/m2]$	lateral earth pressure $\sigma'2$ [kN/m2]	
14 3.25 3.50 20.1 21.6 20.1 21.6 15 3.50 3.75 17.7 19.0 17.7 19.0 16 3.75 4.00 19.0 20.3 19.0 20.3 17 4.00 4.25 20.3 21.7 20.3 21.7 18 4.25 4.50 21.7 23.0 21.7 23.0 19 4.50 4.75 23.0 24.4 23.0 24.4 20 4.75 5.00 24.4 25.7 24.4 25.7 21 5.00 5.25 25.7 27.1 25.7 27.1 22 5.25 5.50 27.1 28.5 27.1 28.5 23 5.50 5.75 28.5 29.8 28.5 29.8 24 5.75 6.00 29.8 31.1 29.8 31.1	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 20 21 22 23	0.00 0.25 0.50 0.75 1.00 1.25 1.50 2.25 2.50 2.75 3.00 3.25 3.50 3.75 4.00 4.25 4.50 4.75 5.00 5.25 5.50	0.25 0.50 0.75 1.00 1.25 1.50 1.75 2.00 2.25 2.25 2.75 3.00 3.25 3.50 3.75 4.00 4.25 4.50 5.50 5.75	0.1 1.7 3.3 5.0 6.6 8.3 9.1 10.6 12.2 13.7 15.3 16.9 18.5 20.1 17.7 19.0 20.3 21.7 23.0 24.4 25.7 27.1 28.5	1.7 3.3 5.0 6.6 8.3 9.9 10.6 12.2 13.7 15.3 16.9 18.5 20.1 21.6 19.0 20.3 21.7 23.0 24.4 25.7 27.1 28.5 29.8	0.1 1.7 3.3 5.0 6.6 8.3 9.1 10.6 12.2 13.7 15.3 16.9 18.5 20.1 17.7 19.0 20.3 21.7 23.0 24.4 25.7 27.1 28.5	1.7 3.3 5.0 6.6 8.3 9.9 10.6 12.2 13.7 15.3 16.9 18.5 20.1 21.6 19.0 20.3 21.7 23.0 24.4 25.7 27.1 28.5 29.8	



Lateral earth pressure

Active earth pressure from soil weight ea [kN/m2]



Active earth pressure from soil weight

Max. $ea = 31.1 \ [kN/m2] \ at \ z = 6.00 \ [m]$, Min. $ea = 0.1 \ [kN/m2] \ at \ z = 0.00 \ [m]$

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PO Box 14001 Richmond Road PO, Calgary AB, Canada T3E 7			
Scale: 344	Title: Lateral earth pressure		

File: Ex3 Date: 26/03/2023

Page No.: | Project: Lateral earth pressure for layered soil (without cohesion)

1.3.5 Example 4: Lateral earth pressure on a wall in sand

1.3.5.1 Description of the problem

For the given soil profile of sand in Figure 15, determine per meter length the following:

- Lateral earth pressure on the wall
- Lateral water pressure on the wall
- Lateral water pressure on the wall due to a surface surcharge load
- Total horizontal force on the wall.

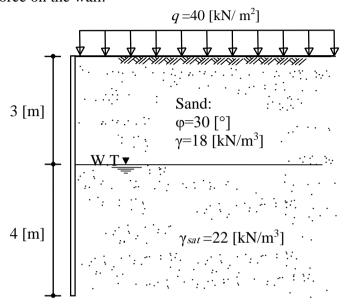


Figure 15 Wall in Sand

1.3.5.2 Lateral Active Earth Pressure

Lateral active earth pressure at point *A* in the soil is equal to the effective vertical stress σ'_{ν} multiplied by a coefficient, $\sigma_h = k_a \sigma'_{\nu}$. If a water table exists, horizontal hydrostatic water pressure is considered. Lateral water pressure at point *A* in the soil is the weight of the water column above that point $w = \gamma_w z$.

Coefficient of lateral active earth pressure is given by:

$$k_a = \frac{1 - \sin 30}{1 + \sin 30} = 0.333$$

The determination of the lateral active earth pressure σ_a is tabulated in 0 and plotted in Figure 7 and Figure 8, while the total lateral earth pressure forces are plotted in Figure 9 and Figure 10.

Table 3 Determination of lateral active earth pressure with depth

	Betermination of fateral active ea		
Depth	lateral active earth pressure	Hydrostatic water	Total lateral active earth
z		pressure	pressure
[m]	$\sigma_a = k_a \sigma'_v$	$w = \gamma_w z$	$E=\sigma_a+w$
	$[kN/m^2]$	[kN/m ²]	$[kN/m^2]$
3	$\sigma_{a1} = k_a \ \sigma'_{v1} = 0.333 \times 54 = 18$	0	18
7	$\sigma_{a2}=k_a \sigma'_{v2}$	$w = \gamma_w h_2$	72.40
/	=18+0.333×4× (22-9.81) =34.25	=9.81×4=39.24	73.49

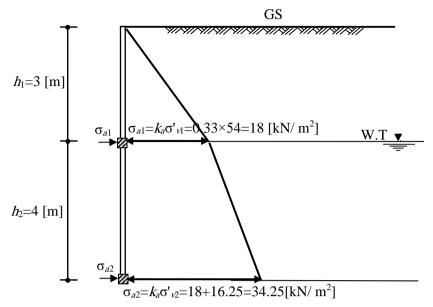


Figure 16 Lateral active earth pressure σ_a

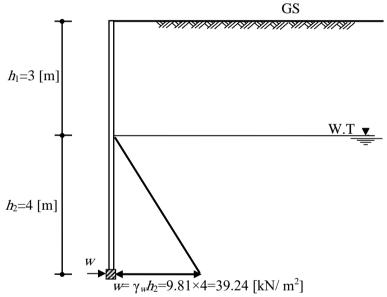


Figure 17 Hydrostatic pressure w

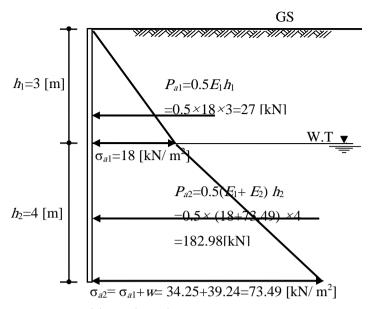


Figure 18 Total lateral earth pressure σ_a and active forces P_a

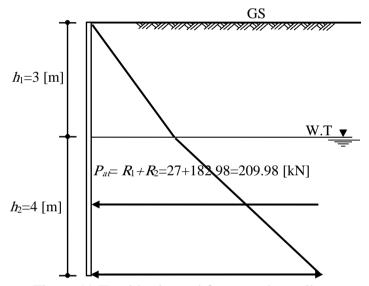


Figure 19 Total horizontal force on the wall P_{at}

1.3.5.3 Lateral earth pressure with a surface surcharge load (fill)

Since the surcharge load (fill) covers an extensive area on the surface, the lateral earth pressure at any point A in the soil increases by $k_a q = 0.333 \times 40 = 13.33$ [kN/m²] due to the weight of the fill, Table 2 and Figure 20.

Table 4 Determination of lateral active earth pressure with depth

Depth	Layer thickness	lateral active earth pressure
z	h	$\sigma_a = k_a \ q + E$
[m]	[m]	$[kN/m^2]$
3	3	$\sigma_{a1} = k_a \ q + k_a \ \sigma'_{v1} = 0.333 \times 40 + 18 = 31.33$
7	4	$\sigma_{a2} = k_a \ q + k_a \ \sigma'_{v2} = 0.333 \times 40 + 73.49 = 86.82$

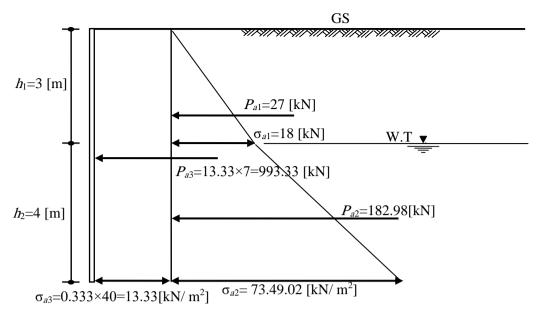


Figure 20 Total lateral earth pressure σ_a and active forces P_a

Figure 21 shows the earth pressures and water presser in a single view

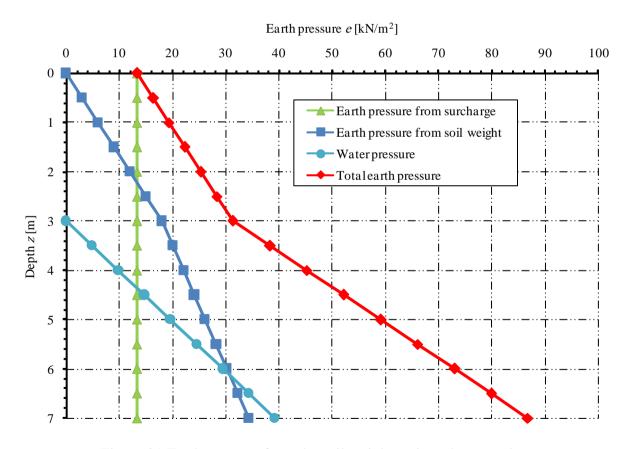


Figure 21 Earth pressure from the soil weight and surcharge and water pressure

1.3.5.1 Lateral earth pressure on a wall in sand by GEO Tools

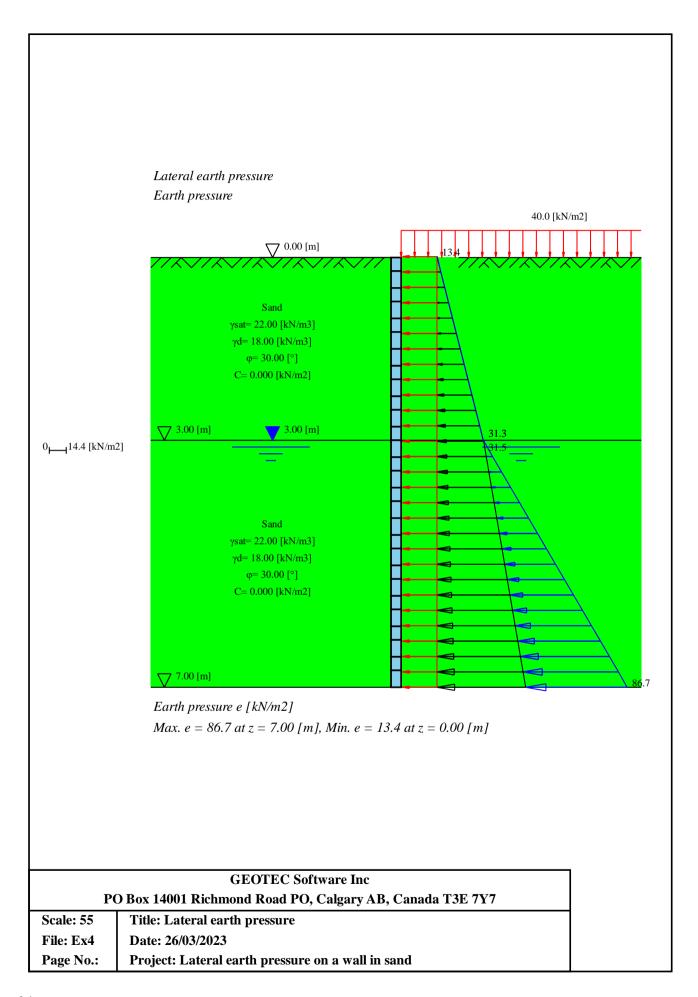
The lateral earth pressure on a wall in sand obtained by *GEO Tools* is equal to that obtained by hand calculation. Also, the input data and results of GEO Tools for this example are presented on the next pages.

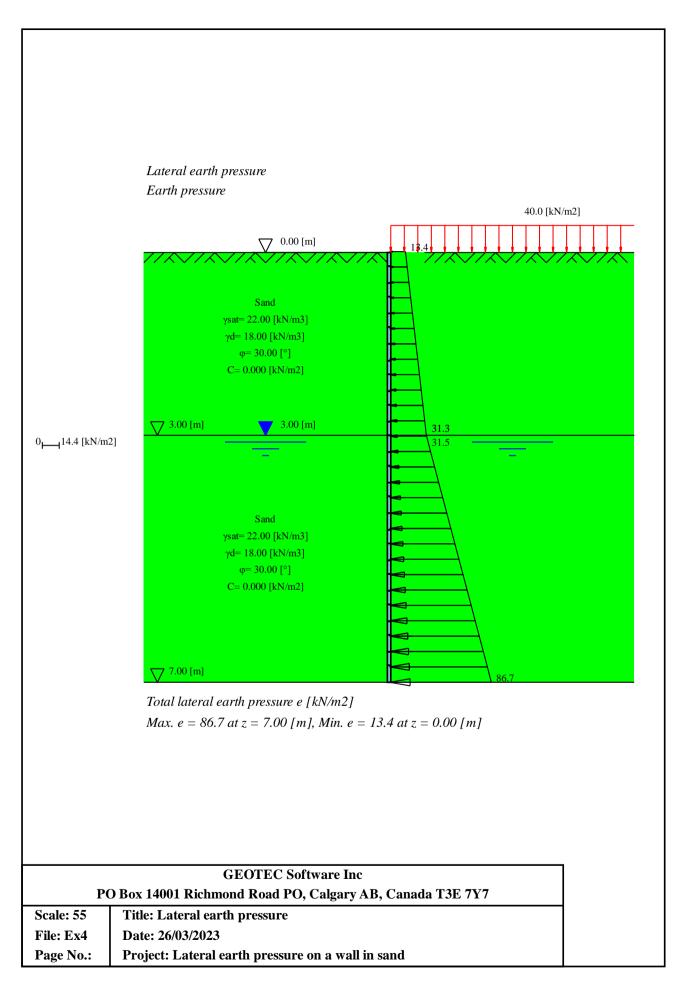
GEO Tools Version 13 Program authors M. El Gendy/ A. El Gendy ************************************						
Lateral earth pressure						
Data: Distributed load Total thickness of soil layers		[kN/m2] [m]				
Element size/ Width of Working Area: Element size Width of Working Area		[m] [m]				
Soil Data: Ground water depth	Gwl	[m]	=	3.00		
Layer No.: 1 Cohesion of the soil Angle of internal friction Dry unit weight of the soil Saturated unit weight of the soil Layer thickness Soil type	φ γd γsat h	[kN/m2] [°] [kN/m3] [kN/m3] [m] [-]	= = =	30.00 18.00 22.00 3.00		
Layer No.: 2 Cohesion of the soil Angle of internal friction Dry unit weight of the soil Saturated unit weight of the soil Layer thickness Soil type	φ γd γsat h	[kN/m2] [°] [kN/m3] [kN/m3] [m] [-]	= = =	30.00 18.00 22.00 4.00		

Result: Resultant R [kN] = 303.7 Location of the resultant from the wall base Y [m] = 2.48

Earth pressures on the sheet pile:

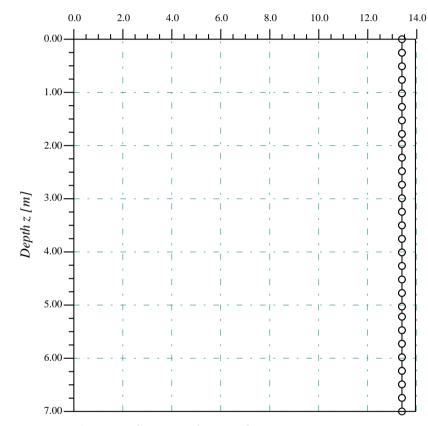
action producted on one officer price.										
No.	Depth	Depth	pressure	earth pressure	earth pressure	earth pressure		Water pressure	lateral earth	lateral earth
			from	from surcharge	from soil	from soil			pressure	pressure
			o ar onar go	our onar go		weight				
I	z1	z2	q1	q2	σz1	σz2	u1	u2	σ'1	σ'2
[-]	[m]		[kN/m2]	-	-	-		[kN/m2]		
1	0.00	0.25	13.3		0.1	1.5	0.0	0.0		
2	0.25	0.50	13.3	13.3	1.5	3.0	0.0	0.0	14.8	16.3
3	0.50	0.75	13.3	13.3	3.0	4.5	0.0	0.0	16.3	17.8
4	0.75	1.00	13.3	13.3	4.5	6.0	0.0	0.0	17.8	19.3
5	1.00	1.25	13.3	13.3	6.0	7.5	0.0	0.0	19.3	20.8
6	1.25	1.50	13.3	13.3	7.5	9.0	0.0	0.0	20.8	22.3
7	1.50	1.75	13.3	13.3	9.0	10.5	0.0	0.0	22.3	23.8
8	1.75	2.00	13.3	13.3	10.5	12.0	0.0	0.0	23.8	25.3
9	2.00	2.25	13.3	13.3	12.0	13.5	0.0	0.0	25.3	26.8
10	2.25	2.50	13.3	13.3	13.5	15.0	0.0	0.0	26.8	28.3
11	2.50	2.75	13.3	13.3	15.0	16.5	0.0	0.0	28.3	29.8
12	2.75	3.00	13.3	13.3	16.5	17.9	0.0	0.0	29.8	31.3
13	3.00	3.25	13.3	13.3	18.0	19.0	0.1	2.5	31.5	34.8
14	3.25	3.50	13.3	13.3	19.0	20.0	2.5	4.9	34.8	38.3
15	3.50	3.75	13.3	13.3	20.0	21.0	4.9	7.4	38.3	41.7
16	3.75	4.00	13.3	13.3	21.0	22.1	7.4		41.7	45.2
17 18	4.00	4.25 4.50	13.3 13.3	13.3 13.3	22.1 23.1	23.1 24.1	9.8 12.3	12.3 14.7	45.2 48.7	48.7 52.1
19	4.25	4.30	13.3	13.3	24.1	25.1	14.7	17.2	48.7 52.1	55.6
20	4.75	5.00	13.3	13.3	25.1	26.1	17.2	19.6	55.6	59.1
21	5.00	5.25	13.3	13.3	26.1	27.1	19.6		59.1	62.5
22	5.25	5.50	13.3	13.3	27.1	28.2	22.1	24.5	62.5	66.0
23	5.50	5.75	13.3	13.3	28.2	29.2	24.5	27.0	66.0	69.5
24	5.75	6.00	13.3	13.3	29.2	30.2	27.0	29.4	69.5	73.0
25	6.00	6.25	13.3	13.3	30.2	31.2	29.4	31.9	73.0	76.4
26	6.25	6.50	13.3	13.3	31.2	32.2	31.9	34.3	76.4	79.9
27	6.50	6.75	13.3	13.3	32.2	33.2	34.3	36.8	79.9	83.4
28	6.75	7.00	13.3	13.3	33.2	34.2	36.8		83.4	





Lateral earth pressure

Active earth pressure from surcharge eq [kN/m2]



Active earth pressure from surcharge

Max. eq = 13.3 [kN/m2] at z = 0.00 [m], Min. eq = 13.3 [kN/m2] at z = 0.00 [m]

GEOTEC Software Inc				
PO Box 14001 Richmond Road PO, Calgary AB, Canada T3E 7Y7				
Scale: 138	Title: Lateral earth pressure			

File: Ex4

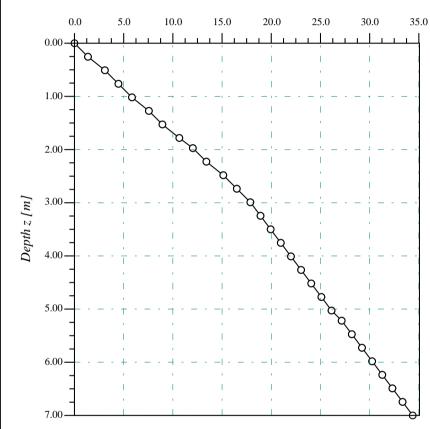
Date: 26/03/2023

Page No.:

Project: Lateral earth pressure on a wall in sand

Lateral earth pressure

Active earth pressure from soil weight ea [kN/m2]



Active earth pressure from soil weight

Max. ea = 34.2 [kN/m2] at z = 7.00 [m], Min. ea = 0.1 [kN/m2] at z = 0.00 [m]

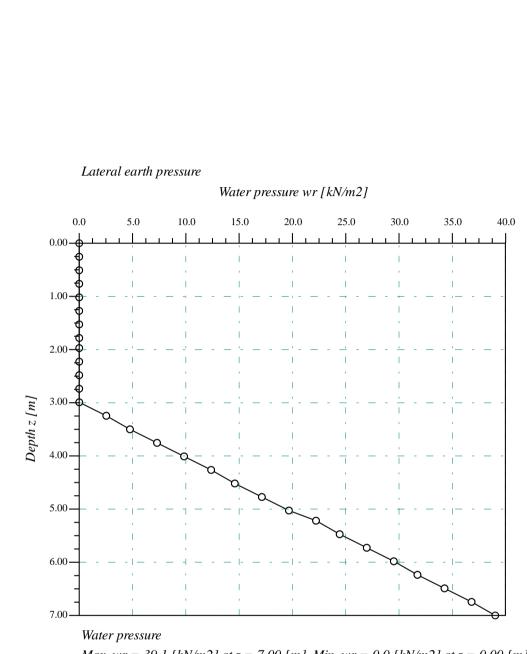
	GEOTEC Software Inc				
 			~ •		

PO Box 14001 Richmond Road PO, Calgary AB, Canada T3E 7Y7

Scale: 344 Title: Lateral earth pressure

File: Ex4 Date: 26/03/2023

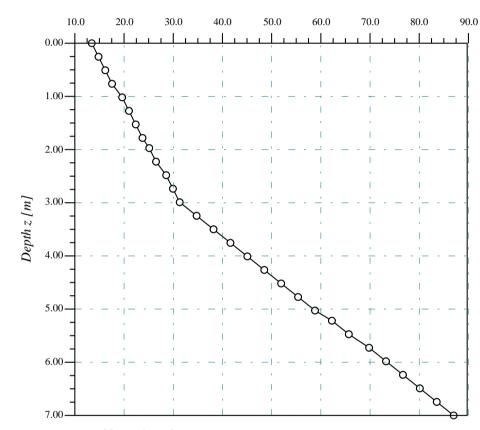
Page No.: | Project: Lateral earth pressure on a wall in sand



Max. wr = 39.1 [kN/m2] at z = 7.00 [m], Min. wr = 0.0 [kN/m2] at z = 0.00 [m]

GEOTEC Software Inc					
PO Box 14001 Richmond Road PO, Calgary AB, Canada T3E 7Y7					
Scale: 317 Title: Lateral earth pressure					
File: Ex4 Date: 26/03/2023					
Page No.: Project: Lateral earth pressure on a wall in sand					

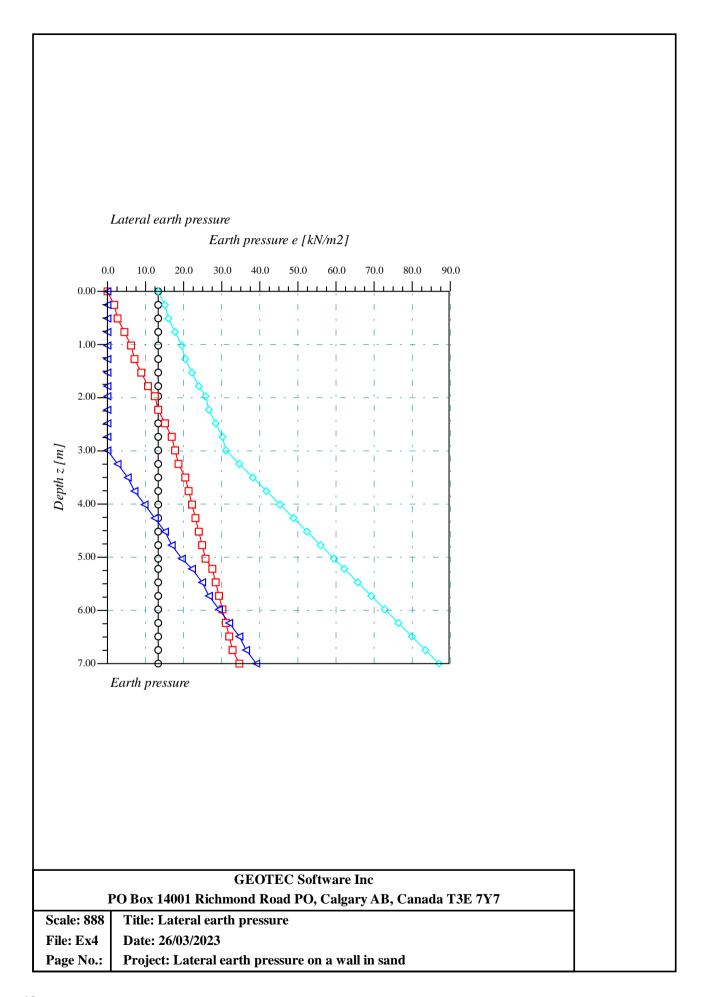
Total lateral earth pressure e [kN/m2]



Total lateral earth pressure

Max. e = 86.7 [kN/m2] at z = 7.00 [m], Min. e = 13.4 [kN/m2] at z = 0.00 [m]

GEOTEC Software Inc					
] 1	PO Box 14001 Richmond Road PO, Calgary AB, Canada T3E 7Y7				
Scale: 688	Scale: 688 Title: Lateral earth pressure				
File: Ex4	File: Ex4 Date: 26/03/2023				
Page No.:	Project: Lateral earth pressure on a wall in sand				



1.3.6 Example 5: Lateral earth pressure on a wall within multi-layered soil

1.3.6.1 Description of the problem

To verify the analysis of lateral earth pressure on walls within multi-layered soil by *Geo Tools*, the active earth pressure diagram obtained by *Bowles* (1996), Example 11-5, Page 606, is compared with that obtained by *Geo Tools*.

Plot the active earth pressure diagram and compute the resultant R and its location y for the wall system shown in Figure 22. This type of problem is often encountered in excavations for large structures where there may be two or more basement levels. The soil parameters φ , φ may be estimated or else be obtained from performing consolidated isotropically undrained (CIU) tests on good-quality tube samples. The major approximation is defining the several strata by abrupt discontinuities (using lines as shown to delineate layers). In most real situations, the soil type grades through a finite length from one to the next.

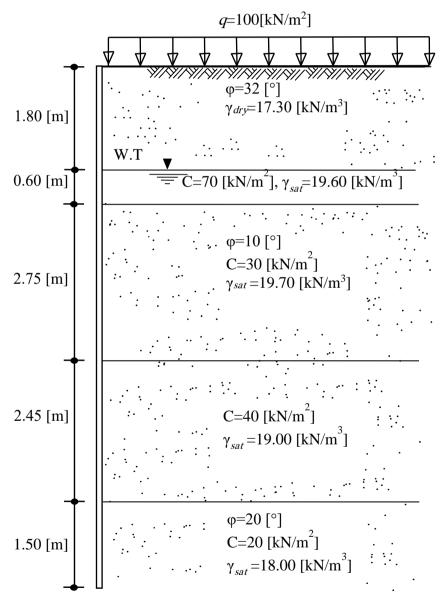


Figure 22 Soil Profile (Bowles 1996)

1.3.6.2 Lateral Active Earth Pressure

The lateral active earth pressure at point A in the soil is quale to the effective vertical stress σ'_{ν} multiplied by a coefficient, $\sigma_h = k_a \sigma'_{\nu}$. If a water table exists, horizontal hydrostatic water pressure is considered. Lateral water pressure at point A in the soil is the weight of the water column above that point $w = \gamma_w z$. Coefficient of lateral active earth pressure is given by:

$$k_a = \frac{1 - \sin \varphi}{1 + \sin \varphi}$$

For instance, for $\varphi = 32^{\circ}$, then, obtain ka = 0.307 and $\sqrt{k_a} = 0.307 = 0.554$, etc.

Typical computations for ΔP ' are as follows (Table 5):

Table 5 Determination of lateral active earth pressure ΔP with depth

Table 3	Determination of fateral active earth pressure 21 with depth
Depth	$\Delta P' = z \gamma$
z	$[kN/m^2]$
[m]	
0	100 [kN/m ²] (surcharge)
1.8	$100+ 1.80(17.30) = 131.4 [kN/m^2]$
2.4	131.4 + 0.6(19.60 - 9.807) = 131.4 + 0.6(9.79) = 137.02 [kN/m2]
5.15	137.02 + 2.75(9.89) = 164.22 etc.

It will be convenient to tabularize the computations as in Table 6 following. Notice that at the interface between two soils, we use the interface pressure two times: first with -dz and the upper ka coefficients, and second with +dz and the ka coefficients of the lower soil. Note also that the $2c\sqrt{ka}$ term can be simplified for the second use. The water pressure is included (ka = kp = kw = 1) if the water cannot drain through the wall or away by other means. Since the water contribution is significant, it is obvious that drainage should be allowed if possible. The tension zone (-) qh is a problem. Should it be included to reduce the wall force or neglected, as it may pull away from the wall? A more conservative case is made if the tension zone is neglected, which we will do here, so neglect the tension zone.

Table 6 Determination of lateral active earth pressure with depth

Soil	Depth	k_a	$\sqrt{k_a}$	$\Delta P' = z\gamma$	Wall pressure	
	z			$[kN/m^2]$	$E==z\gamma k$	
	[m]				$[kN/m^2]$	
1	0	0.307	0.554	100	$100 \times 0.307 = 30.7$	
	1.8- <i>dz</i>			131.14	131.14×0.307 =40.3	
2	1.8+ <i>dz</i>	1.000	1.000	131.14	$131.14 \times 1.00 - 2 \times 70 \times 1.00 = -8.9$	
	2.4- <i>dz</i>			137.02	$137.02 \times 1.00 - 2 \times 70 \times 1.00 = -3.0$	
3	2.4+ <i>dz</i>	0.704	0.839	137.02	$137.02 \times 0.704 - 2 \times 30 \times 0.839 = 46.1$	
	5.15- <i>dz</i>			164.22	164.22×0.704 - 60×0.839 =65.3	
4	5.15- <i>dz</i>	1.000	1.000	164.22	$164.22 \times 1.000 - 2 \times 40 \times 1.00 = 84.2$	
	7.6- <i>dz</i>			186.73	186.73×1.000 - 80×1.00 =106.7	
5	7.6+ <i>dz</i>	0.49	0.700	186.73	$186.73 \times 0.490 - 2 \times 20 \times 0.700 = 63.5$	
	9.1			199.02	199.02×0.490 - 40×0.700 = 69.5	

Figure 23 shows the lateral earth pressures and water presser on the wall according to *Bowles* (1996)

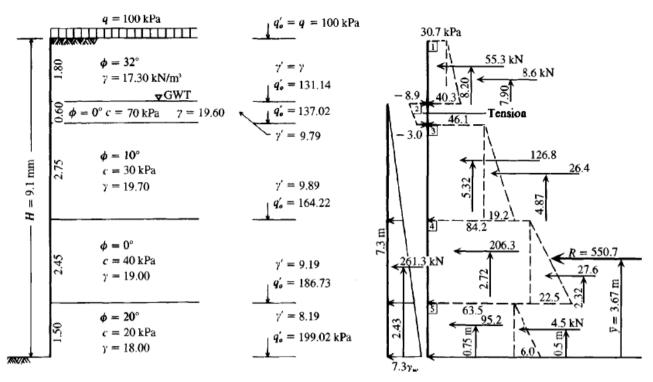


Figure 23 Earth pressure from the soil weight and surcharge and water pressure (Bowles 1996)

1.3.6.3 Lateral earth pressure on a wall in sand by GEO Tools

The lateral earth pressure on the wall within multi-layered soil obtained by *GEO Tools* is equal to that obtained by *Bowles* (1996) through hand calculation. Also, the input data and results of *GEO Tools* for this example are presented on the next pages.

```
*****************
                          GEO Tools
                         Version 13
        Program authors M. El Gendy/ A. El Gendy
Title: Lateral earth pressure on a wall within multi-layered soil
Date: 30-03-2023
Project: Example11-5, Page 606, Foundation Analysis and Design, Bowles 1996
File: Ex5
Lateral earth pressure
Data:
Element size/ Width of Working Area:
                                         Dz [m] = 0.25
Bw [m] = 8.00
Element size
Width of Working Area
Soil Data:
Ground water depth
                                         Gwl [m] = 1.80
Layer No.: 1
Layer No.: 2
Layer No.: 3
Layer No.: 4
Layer No.: 4

Cohesion of the soil

Angle of internal friction

Dry unit weight of the soil

Saturated unit weight of the soil

Layer thickness

\begin{pmatrix}
kN/m2 \\
0
\end{pmatrix} = 40.000

\phi \quad [^{\circ}] = 0.00

\forall d \quad [kN/m3] = 19.00

\forall sat \quad [kN/m3] = 19.00

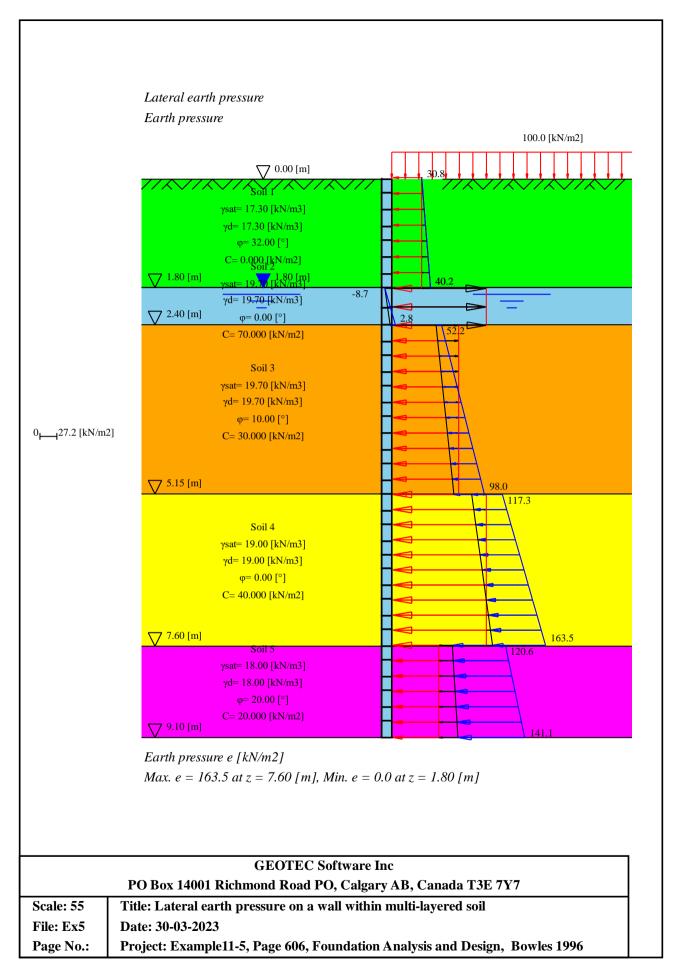
f \quad [m] = 2.45

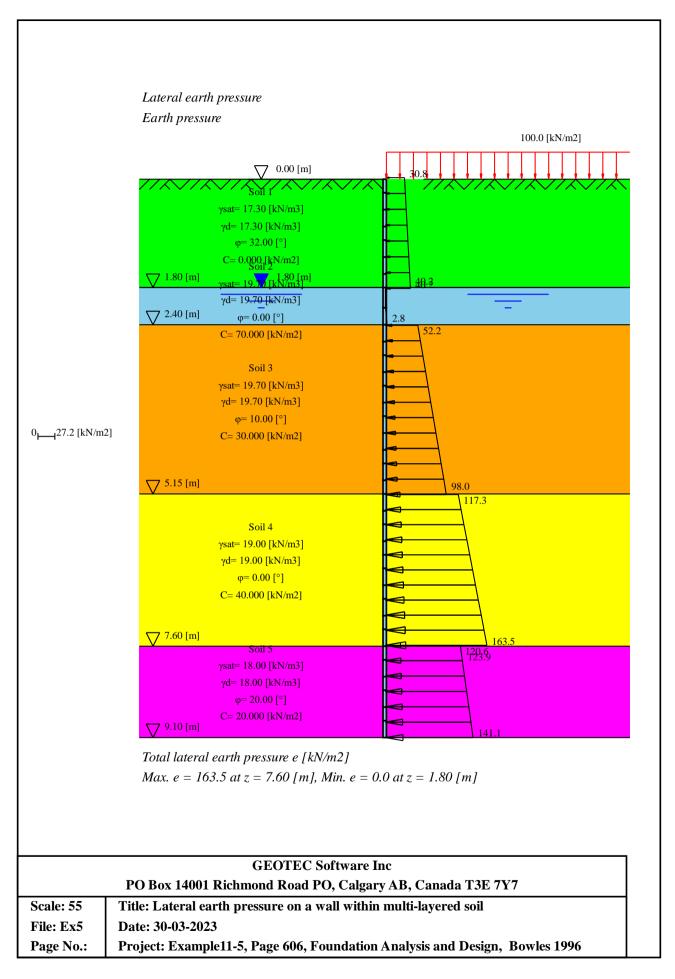
                                          h [m] = 2.45
BOD [-] = Soil 4
Layer thickness
Soil type
Layer No.: 5
Cohesion of the soil
                                         C [kN/m2] = 20.000
                                       \phi [°] = 20.00 \gammad [kN/m3] = 18.00
Angle of internal friction
Dry unit weight of the soil
                                       \gamma d \quad [kN/ms] = 10.00
\gamma sat \quad [kN/m3] = 18.00
h \quad [m] = 1.50
BOD \quad [-] = Soil 5
Saturated unit weight of the soil
Layer thickness
Soil type
```

Result: Resultant R [kN] = 811.3 Location of the resultant from the wall base Y [m] = 3.27

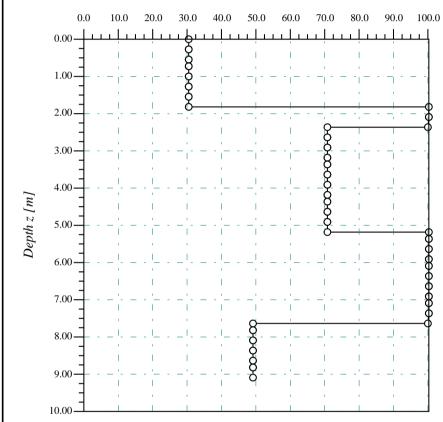
Earth pressures on the sheet pile:

No.	Depth	Depth	Active							
				earth				pressure		
				pressure					earth	earth
			from	irom	irom	from			pressure	pressure
			surcharge	surcharge	SOIL	SOLL				
_	- 1	-2	~1	~?	weight	weight	., 1	2	a.I.1	-12
r 1	[m]	ZZ [m]	q1 [kN/m2]	QZ	021 []-N /m2]	022 []rN /m2]	Ll-M /m21	uz	[]rN /m2]	0 · Z
1	0.00	0.26	30.7 30.7	30.7	0.1	1.4	0.0	0.0	30.8	32.1
2		0.51	30.7	30.7	1.4	2.7	0.0	0.0	32.1	33.4
3	0.51	0.77	30.7 30.7	30.7	2.7	4.1	0.0	0.0	33.4	34.8 36.2
	0.77		30.7	30.7	4.1	5.5	0.0	0.0	34.8	36.2
5	1.03		30.7	30.7	5.5	6.9	0.0	0.0	36.2	37.6
6	1.29	1.54	30.7 30.7	30.7 30.7	6.9	8.2	0.0	0.0	37.6	38.9 40.2
7	1.54	1.80	30.7	30.7	8.2	9.5	0.0	0.0	38.9	40.2
8	1.80	2.10	100.0 100.0	100.0 100.0	-108.8	-105.9 -103.0	0.1	2.9	0.0	0.0
9	2.10	2.40	100.0	100.0	-105.9	-103.0	2.9	5.8	0.0	2.8
10	2.40		70.4	70.4	-24.2	-22.5	6.0	8.3	52.2	56.2
11	2.65	2.90	70.4	70.4 70.4	-22.5 -20.8	-20.8 -19.0	8.3	10.8	56.2 60.4	60.4
12	2.90	3.15	70.4	70.4	-20.8	-19.0	10.8	13.2	60.4	64.6
13	3.15	3.40	70.4 70.4	70.4	-19.0	-17.3 -15.5	13.2	15.7	64.6 68.8	68.8
	3.40	3.65	70.4	70.4	-17.3	-15.5	15.7	18.1	68.8	
15	3.65	3.90	70.4			-13.8	18.1	20.6	73.0	
16	3.90	4.15	70.4		-13.8	-12.1	20.6 23.1	23.1	77.2 81.4	81.4
	4.15	4.40	70.4	70.4	-12.1	-10.3	23.1	25.5	81.4	85.6
	4.40	4.65	70.4	70.4 70.4	-10.3 -8.6	-8.6	25.5 28.0	28.0	85.6 89.8	89.8
	4.65	4.90	70.4	70.4	-8.6	-6.8	28.0	30.4	89.8	94.0
	4.90		70.4	70.4	-6.8	-5.2	30.4	32.8	94.0	98.0
21	5.15	5.39	100.0	100.0	-15.6	-13.4 -11.2	33.0 35.3	35.3	117.3 121.9	121.9
22	5.39		100.0	100.0	-13.4	-11.2	35.3	37.7	121.9	126.4
23	5.64		100.0 100.0	100.0	-11.2	-8.9 -6.7	37.7	40.1	126.4	131.2
24	5.88	6.13	100.0	100.0	-8.9	-6.7	40.1	42.5	131.2	135.7
25		6.37	100.0	100.0	-6.7	-4.4	42.5		135.7	
26	6.37	6.62	100.0 100.0	100.0	-4.4	-2.2 0.0	44.9 47.3	47.3	140.5 145.1	145.1
	6.62	6.86	100.0	100.0	-2.2	0.0	47.3	49.6	145.1	149.6
28	6.86	7.11	100.0 100.0	100.0	0.0	2.3 4.5	49.6 52.1	52.1	149.6	154.4
29	7.11		100.0	100.0	2.3	4.5 6.7	52.1 54.4	54.4	154.4	158.9
30	7.35	7.60	100.0	100.0	4.5	6.7	54.4		158.9	163.5
31	7.60	7.85	49.0 49.0	49.0 49.0	14.6	15.5 16.5	57.0 59.4	59.4	120.6 123.9	123.9
32	7.85	8.10	49.0	49.0	15.5	16.5	59.4	61.8	123.9	127.4
33	8.10	8.35	49.0	49.0 49.0 49.0	16.5	17.5 18.6	61.8	64.3	127.4	130.8
34	8.35		49.0 49.0	49.0	17.5	18.6	64.3 66.7	66.7	130.8	134.3
35	8.60			49.0	18.6	19.6	66.7	69.2	134.3	137.7
	8.85		49.0		19.6	20.5		/1.5		141.1





Active earth pressure from surcharge eq [kN/m2]

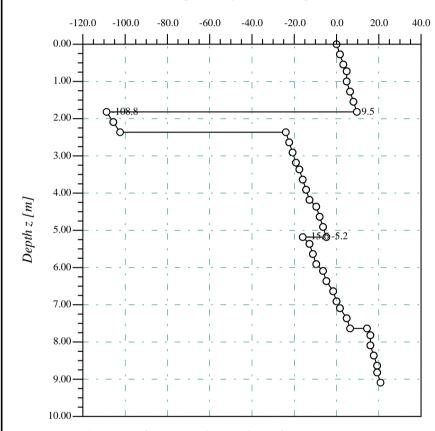


Active earth pressure from surcharge

Max. eq = 100.0 [kN/m2] at z = 1.80 [m], Min. eq = 30.7 [kN/m2] at z = 0.00 [m]

	GEOTEC Software Inc					
	PO Box 14001 Richmond Road PO, Calgary AB, Canada T3E 7Y7					
Scale: 983	Title: Lateral earth pressure on a wall within multi-layered soil					
File: Ex5	Date: 30-03-2023					
Page No.:	Project: Example11-5, Page 606, Foundation Analysis and Design, Bowles 1996					

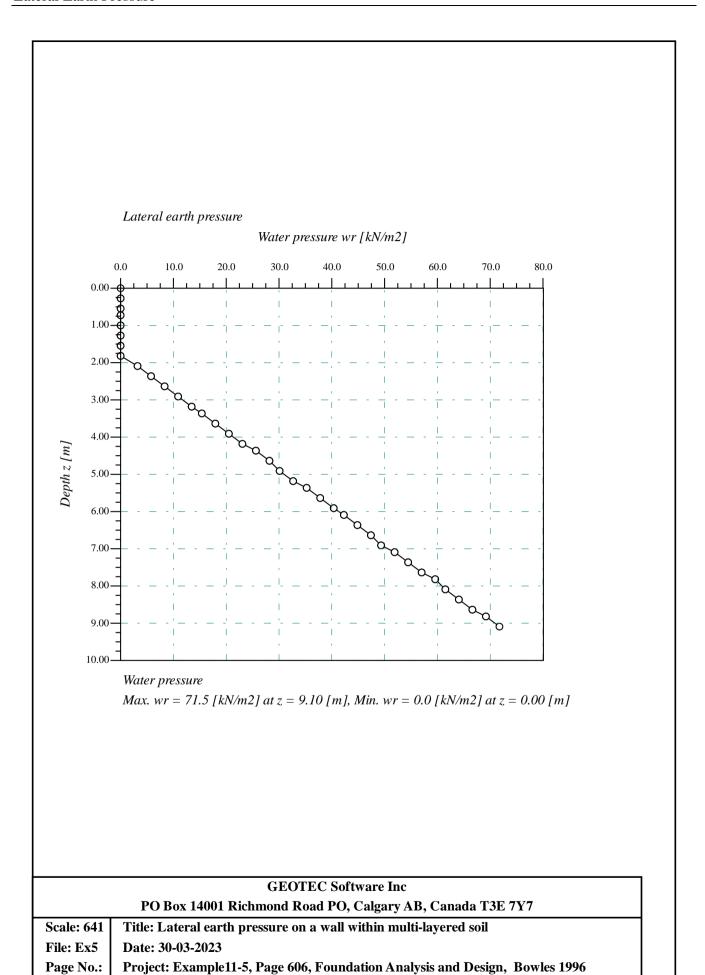
Active earth pressure from soil weight ea [kN/m2]



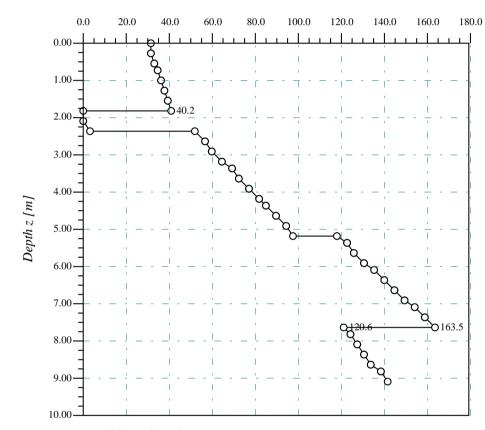
Active earth pressure from soil weight

Max. ea = 20.5 [kN/m2] at z = 9.10 [m], Min. ea = -108.8 [kN/m2] at z = 1.80 [m]

GEOTEC Software Inc					
	PO Box 14001 Richmond Road PO, Calgary AB, Canada T3E 7Y7				
Scale: 1600	Scale: 1600 Title: Lateral earth pressure on a wall within multi-layered soil				
File: Ex5	File: Ex5 Date: 30-03-2023				
Page No.: Project: Example11-5, Page 606, Foundation Analysis and Design, Bowles 1996					



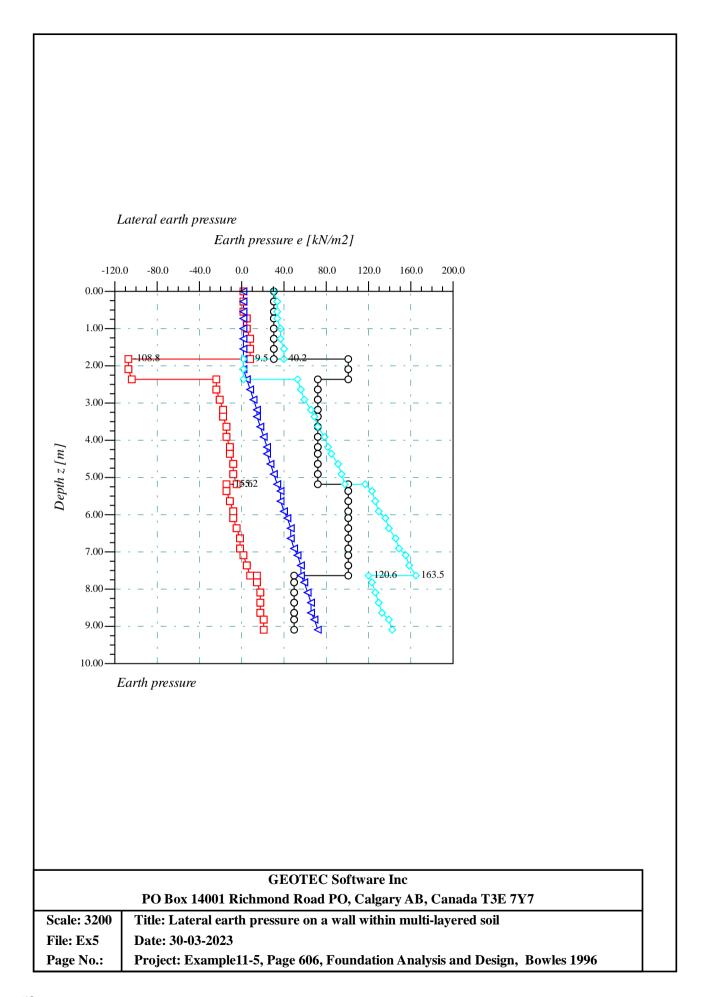
Total lateral earth pressure e [kN/m2]



Total lateral earth pressure

Max. e = 163.5 [kN/m2] at z = 7.60 [m], Min. e = 0.0 [kN/m2] at z = 1.80 [m]

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	PO Box 14001 Richmond Road PO, Calgary AB, Canada T3E 7Y7					
Scale: 1572	Scale: 1572 Title: Lateral earth pressure on a wall within multi-layered soil					
File: Ex5	File: Ex5 Date: 30-03-2023					
Page No.:	Project: Example11-5, Page 606, Foundation Analysis and Design, Bowles 1996					



1.4 References

Bowles, J. (1996): "Foundation Analysis and Design", The McGraw-Hill Companies, Inc.